

## **Mathematics**

**Pre-session course (12 hours)**

*Prof. Michele Longo*

1. *Sets, numbers, and proofs* (C: 1.1, 1.2, 2.1; SB: App. A1, App. A3)
  - 1.1. Vocabulary and operations.
  - 1.2. Relations, functions, and correspondences.
  - 1.3. Real and complex numbers.
  - 1.4. Proofs.
2. *The space  $\mathbb{R}^N$*  (C: 1.3; SB: 10.1-4)
  - 2.1. The algebraic structure of vector space. Inner products and norms on  $\mathbb{R}^N$ . Cauchy-Schwarz inequality.
  - 2.2. Basic topological concepts in Euclidean spaces.
  - 2.3. Sequences on  $\mathbb{R}^N$ .
  - 2.4. Compact and connected sets.
3. *Linear algebra essentials* (C: 1.4; SB: 13.3, 16.1-2, 23.1, 23.3-4, 27.1-6)
  - 3.1. Vector (linear) spaces. Linear combination. Linearly dependent and independent vectors. Basis and coordinates. Dimension.
  - 3.2. Linear functions. Kernel and Image of a linear application. Nonsingular linear functions. Matrix representation of a linear function.
  - 3.3. Eigenvalues and eigenvectors.
  - 3.4. Quadratic forms.

## **References**

- Carl P. SIMON and Lawrence BLUME (SB), *Mathematics for Economists*. W.W. Norton & Company, 1994.
- Michael CARTER (C), *Foundations of Mathematical Economics*, MIT Press, 2001.